

MATHEMATICS

On two new notions of finiteness.

Damir D. Dzhafarov

Eric J. Hall\*

Omar De La Cruz\*

Jean E. Rubin\*

Department of Mathematics  
1395 Mathematical Sciences Building  
Purdue University  
West Lafayette, IN 47907-1395  
E-mail: ddzhafar@math.purdue.edu

We introduce two set-theoretic properties,  $P$  and  $P^*$ , which are definitions of finiteness in the sense that, if the axiom of choice (AC) is assumed, then a set satisfies either property if and only if it is finite. We study the two definitions in set theory without AC and, in particular, derive a relation of implication between the two. We finish by looking at how they relate to the well-known notions of finiteness due to Tarski, Lévy, and Dedekind.